#### Elements of Programming

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Every non-trivial programming language provides:

- primitive expressions representing the simplest elements
- ways to combine expressions
- ways to *abstract* expressions, which introduce a name for an expression by which it can then be referred to.

#### The Read-Eval-Print Loop

Functional programming is a bit like using a calculator

An interactive shell (or REPL, for Read-Eval-Print-Loop) lets one write expressions and responds with their value.

The Scala REPL can be started by simply typing

> scala

#### Expressions

Here are some simple interactions with the REPL

```
scala> 87 + 145
232
```

Functional programming languages are more than simple calcululators because they let one define values and functions:

```
scala> def size = 2
size: => Int
scala> 5 * size
10
```

#### Evaluation

A non-primitive expression is evaluated as follows.

- 1. Take the leftmost operator
- 2. Evaluate its operands (left before right)
- 3. Apply the operator to the operands

A name is evaluated by replacing it with the right hand side of its definition

The evaluation process stops once it results in a value

A value is a number (for the moment)

Later on we will consider also other kinds of values

Here is the evaluation of an arithmetic expression:

(2 \* pi) \* radius

Here is the evaluation of an arithmetic expression:

(2 \* pi) \* radius

(2 \* 3.14159) \* radius

Here is the evaluation of an arithmetic expression:

```
(2 * pi) * radius
```

- (2 \* 3.14159) \* radius
- 6.28318 \* radius

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6.28318 \* radius

6.28318 \* 10

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(2 * pi) * radius
```

```
(2 * 3.14159) * radius
```

6.28318 \* radius

6.28318 \* 10

62.8318

#### Parameters

Definitions can have parameters. For instance:

```
scala> def square(x: Double) = x * x
square: (Double)Double
scala> square(2)
4.0
scala > square(5 + 4)
81.0
scala> square(square(4))
256.0
```

def sumOfSquares(x: Double, y: Double) = square(x) + square(y)
sumOfSquares: (Double,Double)Double

#### Parameter and Return Types

Function parameters come with their type, which is given after a colon

```
def power(x: Double, y: Int): Double = ...
```

If a return type is given, it follows the parameter list.

Primitive types are as in Java, but are written capitalized, e.g:

Int 32-bit integers

Double 64-bit floating point numbers

Boolean boolean values true and false

# **Evaluation of Function Applications**

Applications of parameterized functions are evaluated in a similar way as operators:

- 1. Evaluate all function arguments, from left to right
- 2. Replace the function application by the function's right-hand side, and, at the same time
- 3. Replace the formal parameters of the function by the actual arguments.

sumOfSquares(3, 2+2)

sumOfSquares(3, 2+2)
sumOfSquares(3, 4)

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
9 + square(4)
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
9 + square(4)
9 + 4 * 4
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
9 + square(4)
9 + 4 * 4
9 + 16
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
9 + square(4)
9 + 4 * 4
9 + 16
25
```

### The substitution model

This scheme of expression evaluation is called the *substitution model*.

The idea underlying this model is that all evaluation does is *reduce an expression to a value*.

It can be applied to all expressions, as long as they have no side effects.

The substitution model is formalized in the  $\lambda$ -calculus, which gives a foundation for functional programming.

#### Termination

Does every expression reduce to a value (in a finite number of steps)?

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- Does every expression reduce to a value (in a finite number of steps)?
- ► No. Here is a counter-example

```
def loop: Int = loop
```

loop -> loop -> ....



The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

For instance:

sumOfSquares(3, 2+2)

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
9 + (2+2) * (2+2)
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
9 + (2+2) * (2+2)
9 + 4 * (2+2)
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
9 + (2+2) * (2+2)
9 + 4 * (2+2)
9 + 4 * 4
```

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One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
9 + (2+2) * (2+2)
9 + 4 * (2+2)
9 + 4 * 4
25
```

#### Call-by-name and call-by-value

The first evaluation strategy is known as *call-by-value*, the second is is known as *call-by-name*.

Both strategies reduce to the same final values as long as

- ▶ the reduced expression consists of pure functions, and
- both evaluations terminate.

Call-by-value has the advantage that it evaluates every function argument only once.

Call-by-name has the advantage that a function argument is not evaluated if the corresponding parameter is unused in the evaluation of the function body.

#### Call-by-name vs call-by-value

Question: Say you are given the following function definition:

```
def test(x: Int, y: Int) = x * x
```

For each of the following function applications, indicate which evaluation strategy is fastest (has the fewest reduction steps)

CBV CBN same fastest fastest #steps

0	0	0	test(2, 3)
0	0	0	test(3+4, 8)
0	0	0	test(7, 2*4)
0	0	0	test(3+4, 2*4)

#### Call-by-name vs call-by-value

```
def test(x: Int, y: Int) = x * x
                                           test (7,2*4)
                 test (3+4,8)
test(2, 3)
                                           test(3+4, 8)
                 test (7,8) (3+4)* (3+4)
test(7, 2*4)
test(3+4, 2*4)
                          U
7 × (3+4)
                                           7*7
                                                       49
                  7-*7
  test (2,3)
                             7×1
                                            49
                                                       CISB
                   49
   2*2
                              49
     4
          Samo
                         CRV
```